Vector API design: Selected topics
(flatt values, future shapes, cross-lane motion, snowflakes, atomics)

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http://cr.openjdk.java.net/~jrose/pres/202202-VectorTopics.pdf
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Fitting vectors into bare values — a few ideas
Key observation: Vector lanes are indexed, not selected by name

- A vector is a homogeneous short array
  - A value class is a heterogenous tuple
- Array indexing v[i] requires an in-memory presentation
  - A value class, even if in memory, cannot index its fields
  - Class fields are often, but not always, contiguous
- First compromise: A private multi-field feature in the class loader
  - One field, secretly replicated N times CONTIGUOUSLY
  - (Probably) allocated by JVM after any/all other fields
  - Access (other than to first copy) is via var-handle only
- Additional compromise: Register allocator assigns it a vector register
  - Either automatic, or an extra ad hoc register class annotation

More details: [http://cr.openjdk.java.net/~jrose/values/multi-field.html](http://cr.openjdk.java.net/~jrose/values/multi-field.html)
Example “multi-field” feature

```java
@RegisterAllocation(128) value class Shape128 {
    @MultiField(2) long data;
    //long data#1 ← allocated **contiguously**
}
@RegisterAllocation(256) value class Shape256 {
    @MultiField(4) long data;
    //long data#{1,2,3} ← allocated **contiguously**
}
@RegisterAllocation(512) value class Shape512 {
    @MultiField(8) long data;
    //long data#{1,2,3,4,5,6,7} ← allocated **contiguously**
}
```
Example var-handle based access (HALF-BAKED)

```java
value class Shape512 {
    @MultiField(8) long data;
    private static long OFF_data = U.objectFieldOffset(F_data);
    private static final VarHandle VH_data =
        new VarHandleMultiLongs(Shape512.class, OFF_data, 8);
    public long data(int i) {
        return (long) VH_data.get(this, i);
    }
    public Shape512 dataUpdate(int i, long x) {
        Shape512 pbuf = U.makePrivateBuffer(this);
        VH_data.set(pbuf, i, x);
        return U.finishPrivateBuffer(pbuf);
    } //OR return (Shape512) VH_data.'update'(this, i, x);
}
```
After discussion, the ‘update’ operator doesn’t look so good; use arrays

```java
value class Shape512 {
    @MultiField(8) long data;
    private static long OFF_data = U.objectFieldOffset(F_data);
    private static final VarHandle VH_data =
        new VarHandleMultiLongs(Shape512.class, OFF_data, 8);
    public long data(int i) {
        return (long) VH_data.get(this, i);
    }
    public static Shape512 make(long[] a) { //optimizer makes temporary ‘a’ disappear
        Shape512 pbuf = U.makePrivateBuffer(this);
        for (int i = 0; i < 8; i++)
            VH_data.set(pbuf, i, a[i]);
        return U.finishPrivateBuffer(pbuf);
    }
}
```
Straightforward to expand to multi-vector shapes

```java
@RegisterAllocation(128) value class Shape128x2 {
    @MultiField(2*2) long data;
}
@RegisterAllocation(256) value class Shape256x3 {
    @MultiField(4*3) long data;
}
@RegisterAllocation(512) value class Shape512x4 {
    @MultiField(8*4) long data;
}

// Nested representation would be more complex to implement
value class Shape256x5 {
    @MultiField(5) Shape256 nestedVector;
    // requires carefully contiguous layout of the nestedVectors
}
```
Idea from the group: Maybe have “one size fits most” for polymorphic?

@RegisterAllocation(128) value class Shape128 extends Shape { @MultiField(2) long data; }
@RegisterAllocation(256) value class Shape256 extends Shape { @MultiField(4) long data; }
@RegisterAllocation(512) value class Shape512 extends Shape { @MultiField(8) long data; }

// AND THEN:

@RegisterAllocation(512 /*=MAX*/)
abstract class Shape permits Shape128, Shape256, Shape512 {

// ... models the overlapping zmm/ymm/xmm register file
// with a klass token, maybe useful for polymorphic calling conventions??
The shapes of things to come — rectangles, tiles, matrices
Key observation: Multi-vector algorithms are “a thing”

- Logically rectangular “tiles” (as in the new Intel AMX feature)
  - Show up in optimized “BLAS microkernels” (as in BLIS, GotoBLAS).
  - $C[m,n] += \text{Sum}[k] A[m,k] * B[k,n]$ for $m,n$ small, like lane counts (4/6/8)
  - Key operations: Outer product ($A[*,k]$ against $B[k,*]$), then add into $C[*,*]$ for each $k$
  - Motion along either logical dimension: replicate, reduce, reorder, transpose
  - Loop unrolling: Use “as many registers as you can get away with”
    - Requires testing to see how many that might be (playing “The Price is Right” in vector register file)
    - Easier to configure as a multi-vector shape, not “unroll and jam” of source code
    - This technique combines with tiles: Keep adding tiles until we run out of registers
    - Common operation: Partial reduction (N-way unroll $\Rightarrow$ N-to-1 reduction of accumulator)

- Vector-of-structs: A vector of three-element structs should be three vectors.
  - Common operation: Transpose ($\text{SoV} \Leftrightarrow \text{VoS}$), other ad hoc shuffles.
Some basic operations for multi-vectors

• Native vector species (VLEN1) replicated by some small RLEN, VLEN2=VLEN1 x RLEN
• All the usual lanewise stuff. Also slicing, compression, (full) reduction. Masking (with big masks).
• Shuffle (with a jumbo index array)
  • Some set patterns like transpose, zip/unzip, SoV / VoS
  • Support partial broadcast (a,b,c…) to (a,a,a,b,b,b,c,c,c…) or (a,b,c…,a,b,c…,a,b,c…)
  • Compiles to RLEN single-vector shuffles, possibly with RLEN merges.
  • Partial broadcast can set up an outer product (matrix tile multiply/FMA)
• Reshaping shuffle (expansion/contraction) is probably important
  • Generalizes today’s pick-from-two-vectors shuffle operation
  • Use to extract or insert or broadcast VLEN1-vector against VLEN2 vector
• Striding partial reduction = (a,b,c,d,e,f) to (a+c+e, b+d+f) (reduce by RLEN)
  • Other orders of reduction are best obtained by a previous shuffle?
Challenge problem: BLIS microkernel
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C<6,16> on Haswell
Challenge problem: BLIS microkernel

The Bliss SGEMM microkernel for Haswell is here:
https://github.com/flame/blis/blob/HEAD/kernels/haswell/3/bli_gemm_haswell_asm_d6x8.c#L177

```c
// C<96> += A<16> * B<6>
vbroadcastss(mem(rbx, 6*4), ymm2) vbroadcastss(mem(rbx, 7*4), ymm3)
vfmadd231ps(ymm0, ymm2, ymm4) vfmadd231ps(ymm1, ymm2, ymm5)
vfmadd231ps(ymm0, ymm3, ymm6) vfmadd231ps(ymm1, ymm3, ymm7)
vbroadcastss(mem(rbx, 8*4), ymm2) vbroadcastss(mem(rbx, 9*4), ymm3)
vfmadd231ps(ymm0, ymm2, ymm8) vfmadd231ps(ymm1, ymm2, ymm9)
vfmadd231ps(ymm0, ymm3, ymm10) vfmadd231ps(ymm1, ymm3, ymm11)
vbroadcastss(mem(rbx, 10*4), ymm2) vbroadcastss(mem(rbx, 11*4), ymm3)
vfmadd231ps(ymm0, ymm2, ymm12) vfmadd231ps(ymm1, ymm2, ymm13)
vfmadd231ps(ymm0, ymm3, ymm14) vfmadd231ps(ymm1, ymm3, ymm15)
```
Challenge problem: BLIS microkernel

// C<96> += A<16> * B<6>

var A_SP = FloatVector.SPECIES_256.times(2);  //<16>
var B_SP = FloatVector.SPECIES_64.times(3);   //<6>
var C_SP = FloatVector.SPECIES_256.times(12); //<96>
var C_V = FloatVector.fromArray(C_SP, C_ARR, cIndex); cIndex += 96;
var A_V = FloatVector.fromArray(A_SP, A_ARR, aIndex); aIndex += 16;
var AREPL_V = C_V.broadcastCyclic(A_V);
for (;;) { …
    var B_V = FloatVector.fromArray(B_SP, B_ARR, bIndex);  bIndex += 6;
    var BSPREAD_V = C_V.broadcastExpand(B_V);
    C_V = C_V.fma(AREPL_V, BSPREAD_V);
}
Challenge accepted: Paul Sandoz writes it w/o multi-vectors

https://mail.openjdk.java.net/pipermail/panama-dev/2021-March/012664.html

```java
// Row 0: AB += OldC x beta
AxB_0L = vOldCL.fma(vbr_beta, AxB_0L);
AxB_0R = vOldCR.fma(vbr_beta, AxB_0R);

// Save results to free up registers:
AxB_0L.intoArray(c, c_row_iter);
AxB_0R.intoArray(c, c_row_iter + 8);
c_row_iter += rs_c;

// Row 1: AB += OldC x beta
vOldCL = FloatVector.fromArray(SPECIES_256, c, c_row_iter);
vOldCR = FloatVector.fromArray(SPECIES_256, c, c_row_iter + 8);
AxB_1L = vOldCL.fma(vbr_beta, AxB_1L);
AxB_1R = vOldCR.fma(vbr_beta, AxB_1R);
AxB_1L.intoArray(c, c_row_iter);
AxB_1R.intoArray(c, c_row_iter + 8);
c_row_iter += rs_c;
```
Cross-lane data motion — general observations
Kinds of cross-lane motion

- Random access shuffle: Pulling values to shuffle indexes which attract them.
  - Completely general; use when all else fails or to simulate
- Sidelong slide: Slipping back and forth, maintaining stable order of active set
  - Compress, expand, *sheep-and-goats (bidirectional compress)
  - Useful for quick-sort pivot, collecting conditional loop outputs
  - Compress/expand is useful for parsing (expand regularizes token sizes)
- Sorting/binning: Pushing values to be consistent with key order
  - *Sort, can be simulated by 2lg(N) compress operations (doing radix sort)
  - Complementary to random access shuffle (“reverse data flow”)
  - *Binning is sort followed by reduction of items with the same key
  - For such operations, a key vector drives reordering of a data vector
- Research problem: Co-design of software and hardware
Challenge problems: Parsing (using sidelong compress/expand)

- Load a block of UTF8 bytes
- Find the token boundaries (make a mask)
- Expand tokens to uniform size (24 or 32 bits)
- Perform bit-twiddling to normalize token to UTF16 values
- Compress to 16-bit lanes.
- Profit.

OR:

- Load a block of ASCII characters.
- Find natural language word boundaries.
- Expand tokens to uniform size (8 bytes, = max word size?)
- Strip out punctuation, white space; normalize case; visit the dictionary or histogram…
Appendix: What if my hardware doesn’t do expand natively?

- Expand can be implemented as a by-index permutation (table lookup) plus a horizontal prefix-sum.
- First compute an index vector for the desired expansion.
- The index vector increases monotonically to the left, with a “bump” just after each mask position.
  - Example: Mask (0,0,1,0,0,1,1,0) derives the index vector (0,0,0,1,1,1,2,3).
  - Each index position sums up the total number of mask bits set to the left.
  - May require a series of $\log(N)$ horizontal additions at various (power of two) offsets.
- Then perform a full index-based permutation, using the computed index vector to steer the input values.
  - The monotonically increasing index vector “pulls” each input value “to the right” into the output.
Appendix: OK, so what if my hardware doesn’t do compress natively?

- Compress can be implemented as a masked indexed store (scatter) to a memory temporary.
- First compute an index vector for the desired compression.
- The index vector increases monotonically to the left, with a “bump” just after each mask position.
  - (Same as the index vector for compress, on the previous page!)
  - For unmasked positions, maybe store distinct, non-overlapping placeholder indexes.
  - Example: Mask (0,0,1,0,0,1,1,0) might derive the index vector (-8,-7,0,-6,-5,1,2,-4).
- Then perform a full index-based scatter, using the computed index vector to steer the input values.
  - The output buffer should be extra-sized, with half of the positions usable as “bit buckets” (-8 etc.).
  - If there’s masked store primitive, just mask off the unused indexes, instead of using placeholders.
- After the memory finishes swirling around, pick up the assembled compressed output from the buffer.
  - (Bonus trick: The placeholder indexes suggest how do masked scatters on AVX2 which lacks them.)
Challenge problems: Sorting (the Missing Primitive)

• Load a block of unsorted data
• Pick a pivot (maybe from this block, or maybe from a previous pass)
• Run bidirectional compress to separate across pivot (= Sheep-and-Goats from Hacker’s Delight)
• Store the partitioned sub-blocks, or immediately re-sort (since it’s in registers)
• When tired of sorting, store data for later merging

MUCH LATER…

• Load 2 or more merge blocks
• Perform an all-to-all (outer product) comparison
• Use the resulting bits to steer the merge

BOTH PHASES USE A SORTING OPERATION: How should this be coded?
Challenge problems: Taming the Permutation Zoo

- Most permutations are “not very random”
- Is there some way to describe them concisely so that the compiler can select better instructions?
- Common permutations: zip/unzip, transpose, locally block-wise reordering, talk-to-neighbor (shift/slice)
- How to capture the regular ones? (The optimizer should “see through” shuffle expressions…)
- Connection to multi-vectors: Localized permutations can be expressed as less than $R \lg(R)$ shuffles
  - The general case requires lots of merge-ups ($\lg(R)$ merge tree), but the special ones are simple
  - The very common “partial broadcasts” (cyclic copy, expanding copy) have good locality
- Is there a better notation (transparent to optimizer), than an index vector, for the “easy” permutations?
- Data-driven shuffles (selectFrom lookups) should favor constant lookup tables.
  - Range or bitwise analysis on indexes should routinely remove range checks.
  - Recent case study: [https://mail.openjdk.java.net/pipermail/panama-dev/2022-February/016337.html](https://mail.openjdk.java.net/pipermail/panama-dev/2022-February/016337.html)

RESEARCH PROBLEMS…
Catching snowflakes — getting to odd VPU instructions
Special data types

• Half-float (V)
• Bits128 (CLMUL, AES)
• Complex (many various component types!)

• These can probably be expressed as placeholder types: value objects
• The value object can have a single replicated field

```java
value class ComplexFloat { @MultiField(2) float reim; }
value class ComplexDouble { @MultiField(2) double reim; }
value class Bits128 { @MultiField(2) long bits; }
value class Float16 { short bits; }
```
Special operations

- Carry-less multiply [p]clmul (V+S)
- aesenc/aesdec steps (V+S)
- vp2intersect: all-to-all (outer product) comparison with dual-dimension mask reduction
- vnni: 8/16b precision dot product, 32b precision accumulation (saturating!)
- AMX (matrix tiles); tile multiplication, dot product (like vnni)
- FMA, sometimes with odd parameter order or alternating add+sub variation
- Bit-permutation
  - PDEP, PEXT (S only, not V)
  - Reverse bits, reverse bytes, (rotate? transpose?)
- many ad hoc permutations and special loads (too many to keep track of)
  - vpermi1ps (simple butterfly-like shift within 128-bit mega-lanes); vperm2f128
Suggestion: Incubate snowflake intrinsics in JVM-only package

```java
package jdk.internal.vm.data;

@RegisterAllocation(128) public value class Bits128 {
    private @MultiField(2) lo_hi;
    public static Bits128 make(long hi, long lo) { ... }

    public static Bits128 bitwiseAnd(Bits128 a, Bits128 b) { ... }
    public static Bits128 bitwiseOr(Bits128 a, Bits128 b) { ... }
    public static Bits128 bitwiseXor(Bits128 a, Bits128 b) { ... }

    public static Bits128 multiplyFull(long a, long b) { ... }
    public static Bits128 multiplyCarryless(long a, long b) { ... }
    public static Bits128 aesEncodeStep(Bits128 state, Bits128 key) { ... }
}
```
Suggestion: Incubate nascent new primitive and vector types similarly

```java
package jdk.internal.vm.data.halffloat;

public class HalfFloat { ...
    public static HalfFloat add(HalfFloat a, HalfFloat b) { ... }
    public static HalfFloat sub(HalfFloat a, HalfFloat b) { ... }
    public static HalfFloat mul(HalfFloat a, HalfFloat b) { ... }
    public static HalfFloat sqrt(HalfFloat a) { ... }
}

public class HalfFloatVector extends AbstractVector<HalfFloat> { ... }
public class HalfFloat128Vector extends HalfFloatVector { ... }
public class HalfFloat256Vector extends HalfFloatVector { ... }
public class HalfFloat512Vector extends HalfFloatVector { ... }
```
Half-baked suggestion: Incubate nascent vector lane operations

package jdk.internal.vm.data;

public class ExtraVectorOperators extends VectorOperators {
    public static final Associative ADD_HALF_FLOAT = ...;
    public static final Binary AES_ENC_STEP = ...;
    public static final Binary CL_MUL_HI = ...;
    public static final Binary CL_MUL_LO = ...;
}

// Not clear this pans out. The point is a proving ground for ad hoc ops.
Vector atomics
— what might be useful
The underlying realities of memory operations (an educated guess)

• Memory travels in cache blocks (with update masks)
• The CPU decomposes cache operations into smaller units, tracking data as scalars (words, bytes, …)
• Existing locking operations briefly pin cache blocks and suppress decomposition
  • Sometimes they pin adjacent blocks when a locked operation crosses a line

• Presumably there are difficulties with suppressing decomposition of vectors
  • Decomposing memory operations supports value numbering and reordering
  • Suppressing decomposition breaks those optimizations
  • Decomposing operations also allows more flexible fit to internal queue limits
  • Suppressing decomposition requires more resource allocation for internal queues

• Still, it is possible, in principle, to consider cache-locked versions of vector operations
What cache-locked vector operations might look like

- Locked vector load, unmasked
  - Allocate any load queue resources, lock one or two cache lines
  - Transfer indicated data lanes into value tracking registers; release cache
- Locked vector load, masked — similar to unmasked
  - Might lock only one cache line where unmasked would lock two
- Locked vector store, unmasked
  - Fetch unwritten parts of cache line(s), wait for all CPU data ready
  - Allocate any store queue resources, lock one or two cache lines
  - Drain store queue entries under lock; release cache
- Locked vector store, masked — similar to unmasked
  - Might lock only one cache line
Existing instructions that might help

- `movdqa/movdqu`: Maskable; transfers up to 512 bits. Not lockable?
  - *Mostly* atomic? (Therefore *slightly* non-atomic.)
  - (Very Naive Feature Request: Allow these guys to be lock-prefixed!)
- `lock cmpxchg16b`: Works on *aligned* 64-bit word pairs. Slow. Improvable?
  - Could possibly help with 2-word value types.
  - Might be usable as a plain atomic load if an impossible test-value is set up.
  - Might be usable as a plain atomic store if a likely test-value is set up.
- `movdir64b`: Direct cache-bypassing store for 512 bits. Slow; requires fence.
  - Write-atomic, aligned. Not read-atomic; no support for reads.
  - `movdiri`: Like `movdir64b`, but 32/64 bits. Cache-bypassing, requires fence.
- TSX instructions: Rocky history. Excessive power: multiple cache lines (DCAS/MCAS).
What cache-locked vector CAS might look like

- Two vectors A, B, one mask K, one address M, returns C
  - Allocate any queue resources, lock one or two cache lines
  - Load C=(M){K}, compare to C and A under mask K
  - Store (M){K}=B under mask, but only if C{K}=A{K}
  - Drain queues; release cache

- Two vectors A, B, *two* masks K, K2, one address M, returns C
  - Similar to above, but store (M){K2}=B under *second* mask
  - Possible restriction: test mask K is limited in size/shape

- Memory transaction is always one or two-adjacent cache lines
  - Not a general DCAS/CAS2; more like a “whole cache line” CAS
  - Similar also to CMPXCHG16B, probably slow like that one.
Use cases

- Java volatile variable, with flat value >64 bits.
  - Struct-tearing is a (rare) possibility to protect against
  - Alternative to SW transactional memory (side-locks)
- Java extended VarHandle operations, on flat value >64 bits.
- Reading/writing/linking inter-thread communication or coprocessor command blocks (in user space)
- Concurrent version control on the same cache line (nR/1W SeqLock, for example).

- The alternative is object versioning: Use an indirection, CAS-patch a 64-bit pointer to current version.
- For Java volatiles, each version of the variable is a freshly allocated “buffer” object.
- One cost: Indirection harms locality (extra cache-line fetches).
- Another cost: Garbage collector has to go around cleaning up unused indirection blocks.
Plan of record

- Rely *only* on 64-bit memory atomicity.
- When in doubt, use object versioning, extra buffering, indirections.
- Invest more aggressively in one-word representations.
  - Example: value class Optional<T> { Object valOrSentinel; }
  - Instead of: value class Optional<T> { T val; boolean isPresent; }

- (Any guidance from the hardware gurus?)
Thank You

Questions? Comments?
http://cr.openjdk.java.net/~jrose/pres/202202-VectorTopics.pdf
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